

PRINCIPLES - LESSON 100

DIVIDING POWERS WITH LIKE BASES / FRACTIONS TO POWERS

Simplify.

$$\text{ex1) } (x^6)^3 = x^{6 \cdot 3} = \boxed{x^{18}}$$

$$\text{ex2) } x^4 \cdot x^8 = x^{4+8} = \boxed{x^{12}}$$

$$\text{ex3) } (-1x^2y^3z^5)^7 = (-1)^7 (x^2)^7 (y^3)^7 (z^5)^7$$
$$= \boxed{-1x^{14}y^{21}z^{35}}$$

FIND THE RULE

Simplify.

ex4) $\frac{y^5}{y^2} = \frac{\cancel{y \cdot y \cdot y \cdot y \cdot y}}{\cancel{y \cdot y}} = \frac{y^3}{1} = \boxed{y^3}$

ex5) $\frac{a^4 b^7}{ab^4} = \frac{\cancel{a \cdot a \cdot a \cdot a} \cdot \cancel{b \cdot b \cdot b \cdot b \cdot b \cdot b \cdot b}}{\cancel{a} \cdot \cancel{b \cdot b \cdot b \cdot b}} = \frac{a^3 b^3}{1} = \boxed{a^3 b^3}$

DIVIDING POWERS WITH LIKE BASES

Shortcut to dividing powers with like bases:

SUBTRACT EXPONENTS

Exponent Rule 4: Dividing Powers with Like Bases

$$\frac{x^m}{x^n} = x^{m-n}$$

DIVIDING POWERS WITH LIKE BASES

Simplify.

ex6)
$$\frac{x^4 y^2 z^6}{x^2 y z^3} = \frac{x^2 y z^3}{1} = \boxed{x^2 y z^3}$$

ex7)
$$\frac{2a^7 b^2 c}{4a^5 b^6} = \boxed{\frac{1a^2 c}{2b^4}}$$

Reduce coefficients first!

$$\frac{2}{4} = \frac{1}{2}$$

FIND THE RULE

Simplify.

$$\begin{aligned} \text{ex8)} \quad \left(\frac{1}{2}\right)^3 &= \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1 \cdot 1 \cdot 1}{2 \cdot 2 \cdot 2} = \frac{(1)^3}{(2)^3} \\ &= \boxed{\frac{1}{8}} \end{aligned}$$

$$\begin{aligned} \text{ex9)} \quad \left(\frac{3a}{4b^3}\right)^2 &= \frac{3a}{4b^3} \cdot \frac{3a}{4b^3} = \frac{(3a)^2}{(4b^3)^2} = \boxed{\frac{9a^2}{16b^6}} \end{aligned}$$

FRACTIONS TO POWERS

Shortcut to raising fractions to powers:

**RAISE NUMERATOR AND
DENOMINATOR SEPARATELY
TO THE EXPONENT**

Exponent Rule 5: Fractions to Powers

$$\left(\frac{x}{y}\right)^m = \frac{(x)^m}{(y)^m}$$

FRACTIONS TO POWERS

Simplify.

$$\begin{aligned} \text{ex10)} \quad \left(\frac{2d^3}{3e^5} \right)^2 &= \frac{(2d^3)^2}{(3e^5)^2} = \frac{(2)^2(d^3)^2}{(3)^2(e^5)^2} \\ &= \boxed{\frac{4d^6}{9e^{10}}} \end{aligned}$$

LAWS OF EXPONENTS

Simplify.

$$\begin{aligned} \text{ex11)} \quad \left(\frac{-4c^5}{2c^3} \right)^3 &= \left(\frac{-2c^2}{1} \right)^3 = (-2c^2)^3 \\ &= (-2)^3 (c^2)^3 \\ &= -8c^6 \end{aligned}$$

**Before raising a fraction to a power,
first simplify the fraction completely.**

LAWS OF EXPONENTS

Simplify.

$$\begin{aligned} \text{ex12)} \quad & \left[\frac{-3j^4k^6}{(6jk)^2} \right]^2 = \left[\frac{-3j^4k^6}{36j^2k^2} \right]^2 = \left[\frac{-1j^2k^4}{12} \right]^2 \\ & = \frac{(-1j^2k^4)^2}{(12)^2} \\ & = \frac{1j^4k^8}{144} \end{aligned}$$

Before raising a fraction to a power, first simplify the fraction completely.

Don't forget about PEMDAS!