

# PRINCIPLES - LESSON 12A

## PRIME FACTORIZATION

**PRIME NUMBER:** a number with exactly 2 positive factors (1 and itself)

**From our definition, why is the number 1 NOT a prime number?**

**The number 1 has only one positive factor. (itself)**

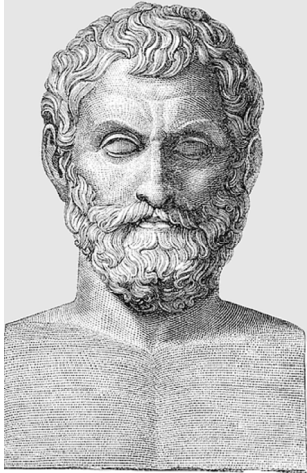
**What makes the number 2 unique as a prime number?**

**The number 2 is the first and only even prime number.**

**What do we call numbers that have more than 2 factors?**

**Numbers with more than 2 factors are called **COMPOSITE NUMBERS.****

# THE SIEVE OF ERATOSTHENES



**ERATOSTHENES OF CYRENE ( 276 B.C. - 194 B.C. )**

**ancient mathematician, geographer, poet, astronomer,  
music theorist, and chief librarian of the Library of Alexandria**

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**SIEVE OF ERATOSTHENES**

# PRIME FACTORIZATION

**PRIME FACTORIZATION:** every composite number can be written as a unique product of prime numbers

In this way, prime numbers are the building blocks for all other numbers.

ex1) Find the prime factorization of 18.

$$\begin{array}{c} 18 \\ / \quad \backslash \\ 9 \quad 2 \\ / \quad \backslash \\ 3 \quad 3 \end{array} = 2 \cdot 3 \cdot 3 = 2 \cdot 3^2$$

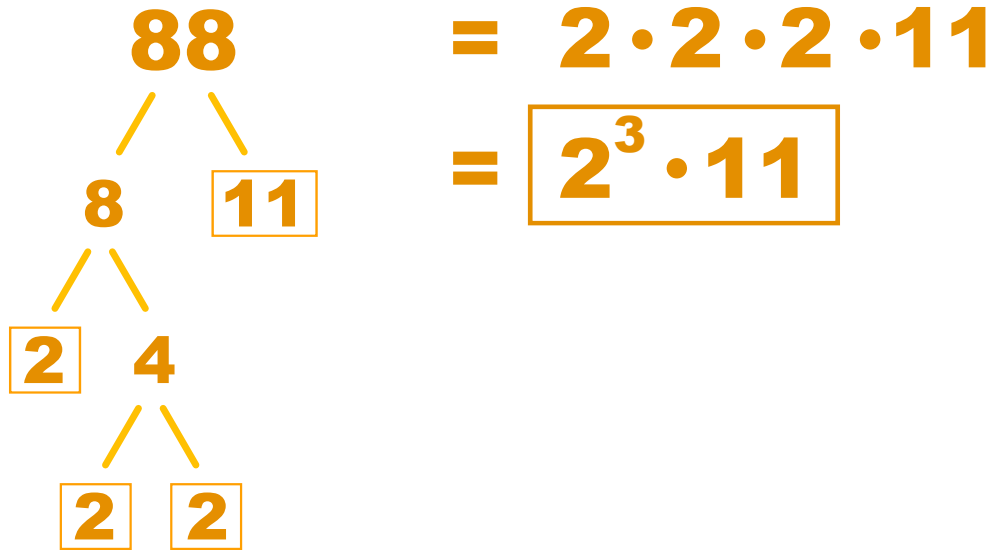
# PRIME FACTORIZATION

ex2) Find the prime factorization of 52.

$$\begin{array}{l} 52 \\ / \quad \backslash \\ 4 \quad 13 \\ / \quad \backslash \\ \boxed{2} \quad \boxed{2} \end{array}$$
$$= 2 \cdot 2 \cdot 13$$
$$= \boxed{2^2 \cdot 13}$$

# PRIME FACTORIZATION

ex3) Find the prime factorization of 88.



# DIVISIBILITY RULES

**A number is divisible by 2 if**

**the last digit is divisible by 2**

**A number is divisible by 3 if**

**the sum of the digits is divisible by 3**

**A number is divisible by 4 if**

**the last 2 digits are divisible by 4**

**A number is divisible by 5 if**

**the last digit is 0 or 5**

**A number is divisible by 6 if**

**it is divisible by both 2 and 3**

**A number is divisible by 7 if**

**your calculator says so**

**A number is divisible by 8 if**

**the last 3 digits are divisible by 8**

**A number is divisible by 9 if**

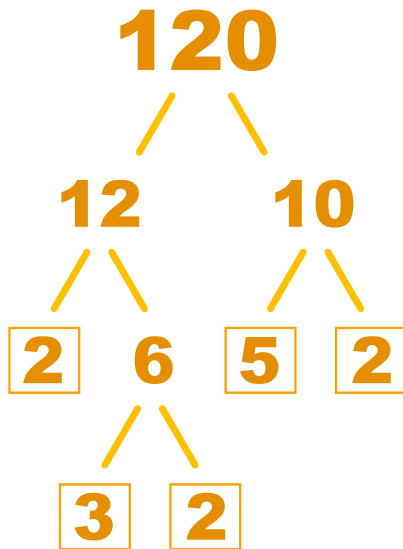
**the sum of the digits is divisible by 9**

**A number is divisible by 10 if**

**the last digit is zero**

# PRIME FACTORIZATION

ex4) Find the prime factorization of 120.



$$= 2 \cdot 2 \cdot 2 \cdot 3 \cdot 5$$

$$= \boxed{2^3 \cdot 3 \cdot 5}$$

# PRIME FACTORIZATION

ex5) Find the prime factorization of 1524.

$$\begin{array}{c} 1524 \\ / \quad \backslash \\ 254 \quad 6 \\ / \quad \backslash \quad / \quad \backslash \\ 127 \quad 2 \quad 3 \quad 2 \end{array} \quad = \quad 2 \cdot 2 \cdot 3 \cdot 127$$
$$= \boxed{2^2 \cdot 3 \cdot 127}$$



# PRIME FACTORIZATION

**ex6) Find the prime factorization of 227.**

**227** is a prime number.

# PRIME FACTORIZATION

You must check all prime numbers up to the

**SQUARE ROOT**

of the number for divisibility.