

PRINCIPLES - LESSON 14C

MULTIPLYING RADICALS

Simplify.

$$\text{ex1) } 5 \cdot \sqrt{3} = \boxed{5\sqrt{3}}$$

$$\text{ex2) } 5 \cdot \sqrt{4} = 5 \cdot 2$$
$$= \boxed{10}$$

$$\text{ex3) } \sqrt{5} \cdot \sqrt{4} = \sqrt{5} \cdot 2$$
$$= \boxed{2\sqrt{5}}$$

THE GROUND RULES

Ground Rule #1:

**"Inside with Inside -
Outside with Outside"**



When multiplying radicals, multiply numbers inside a radical only by other numbers inside a radical. Multiply numbers outside a radical only by other numbers outside a radical.

MULTIPLYING RADICALS

Simplify.

$$\text{ex4) } \sqrt{8} \cdot \sqrt{2}$$

THE EASY WAY

$$= \sqrt{8 \cdot 2} = \sqrt{16} = \boxed{4}$$

$$\text{ex5) } \sqrt{8} \cdot \sqrt{2}$$

THE HARD WAY

$$= \sqrt{4 \cdot 2} \cdot \sqrt{2}$$

$$= 2\sqrt{2} \cdot \sqrt{2}$$

$$= 2\sqrt{4} = 2 \cdot 2 = \boxed{4}$$

THE GROUND RULES

Ground Rule #2:

How to Multiply
Radicals



$$\sqrt{a} \cdot \sqrt{b} = \sqrt{ab}$$

(true for all real numbers)

MULTIPLYING RADICALS

Simplify.

$$\text{ex6) } \sqrt{2n^5} \cdot \sqrt{6n}$$

$$= \sqrt{2n^5 \cdot 6n}$$

$$= \sqrt{12n^6}$$

$$= \sqrt{4 \cdot 3 \cdot n^6}$$

$$= \boxed{2n^3\sqrt{3}}$$

$$\text{ex7) } 3\sqrt{5xy} \cdot 2\sqrt{4xy^4}$$

$$= 3 \cdot 2 \cdot \sqrt{5xy \cdot 4xy^4}$$

$$= 6\sqrt{4 \cdot 5 \cdot x^2 \cdot y^4 \cdot y}$$

$$= \boxed{12xy^2\sqrt{5y}}$$

MULTIPLYING RADICALS

Simplify.

ex8) $5\sqrt[3]{9x^2} \cdot 2\sqrt[3]{-3x^5}$

Now we need perfect cubes!

$$= 10\sqrt[3]{-27x^7}$$

$$= 10\sqrt[3]{-27 \cdot x^6 \cdot x}$$

$$= \boxed{-30x^2\sqrt[3]{x}}$$

MULTIPLYING RADICALS

Simplify.

$$\text{ex9) } \sqrt{3} (\sqrt{3} + 5)$$

$$= \sqrt{9} + 5\sqrt{3}$$

$$= \boxed{3 + 5\sqrt{3}}$$

MULTIPLYING RADICALS

Simplify.

FOIL

ex10) $(2\sqrt{5} + 4)(4\sqrt{5} - 7)$

$$= 8\sqrt{25} - 14\sqrt{5} + 16\sqrt{5} - 28$$

$$= 40 + 2\sqrt{5} - 28$$

$$= 12 + 2\sqrt{5}$$

MULTIPLYING RADICALS

Simplify.

**NOT
FOIL**

ex11) $(-6\sqrt{w})^2$

$$= (-6\sqrt{w})(-6\sqrt{w})$$

$$= 36\sqrt{w^2}$$

$$= \boxed{36w}$$

FOIL

ex12) $(1-6\sqrt{w})^2$

$$= (1-6\sqrt{w})(1-6\sqrt{w})$$

$$= \overset{F}{1} - \overset{O}{6\sqrt{w}} - \overset{I}{6\sqrt{w}} + \overset{L}{36\sqrt{w^2}}$$

$$= \boxed{1 - 12\sqrt{w} + 36w}$$