

PRINCIPLES - LESSON 7B

THE SLOPE-INTERCEPT FORM

Recall: Slope is a measure of steepness.

$$\text{SLOPE} = \frac{\text{rise}}{\text{run}}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Positive Slope:



Zero Slope:



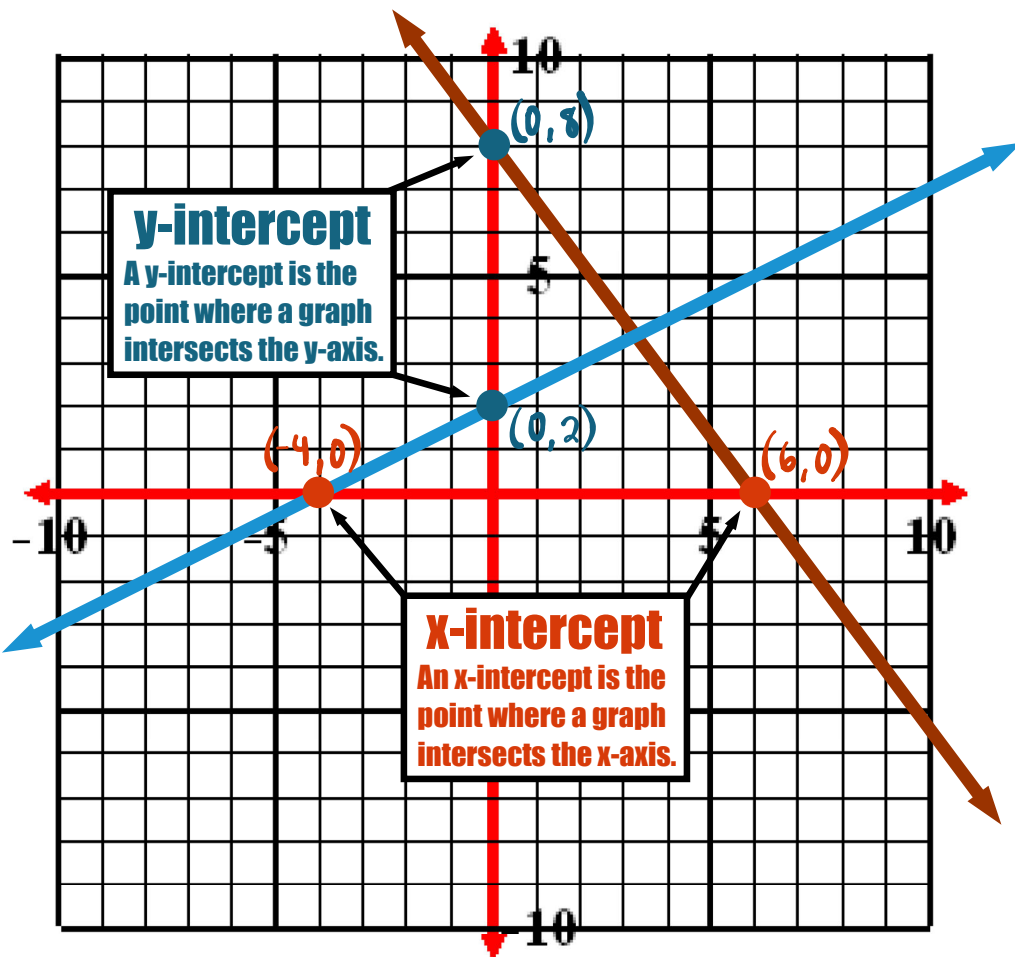
Negative Slope:



Undefined Slope:



FINDING INTERCEPTS



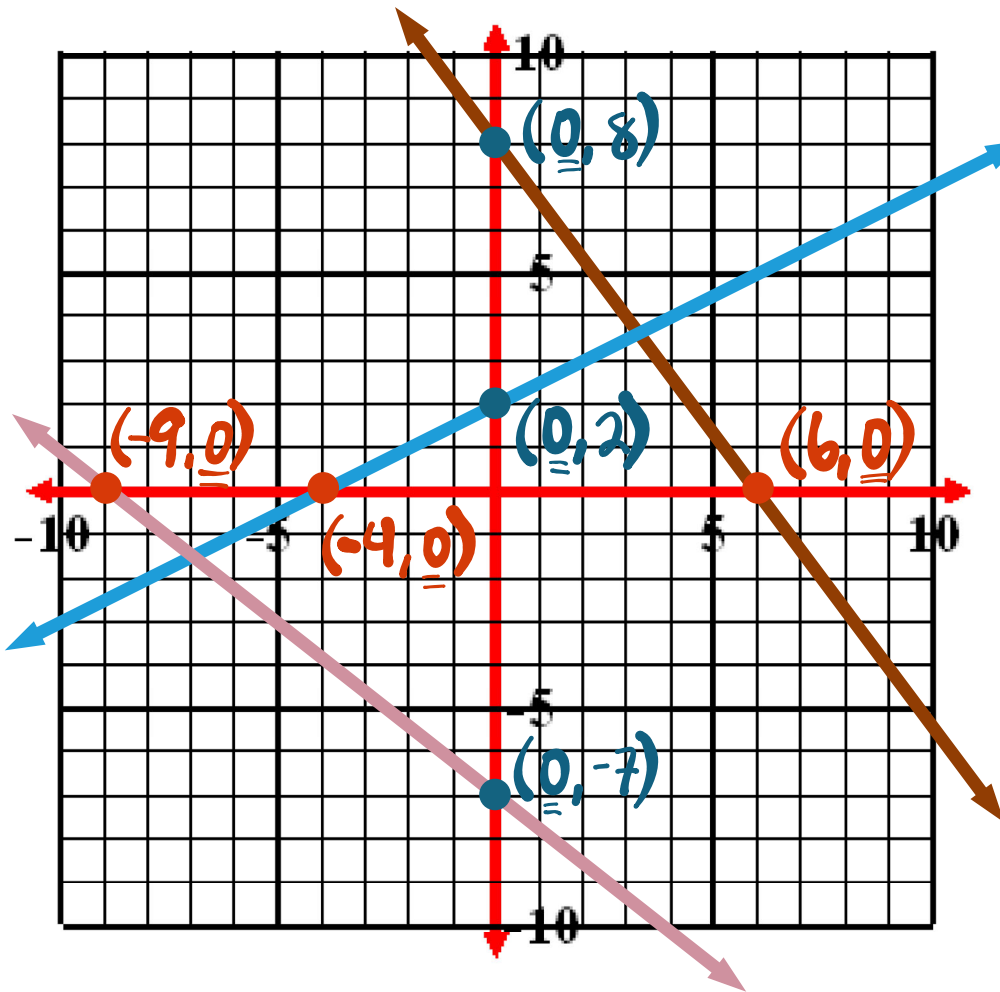
x-int: $(-4, 0)$

y-int: $(0, 2)$

x-int: $(6, 0)$

y-int: $(0, 8)$

INTERCEPTS



What do all x-intercepts have in common?

All x-intercepts have a y-coordinate of ZERO.

What do all y-intercepts have in common?

All y-intercepts have a x-coordinate of ZERO.

EXPLORATION

Make a table and graph each equation. Find the slope and y-intercept.

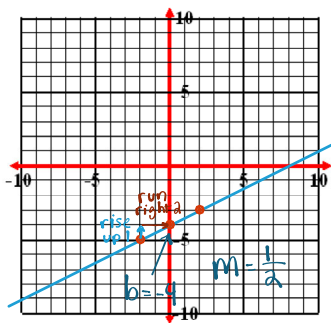
ex1) $y = \frac{1}{2}x - 4$

$m = \frac{1}{2}$

slope = $\frac{\text{rise}}{\text{run}}$

Choose 2 points on the line and determine the rise and run between them.

X	Y
0	-4
2	-3
-2	-5



(y-intercept) $b = -4$

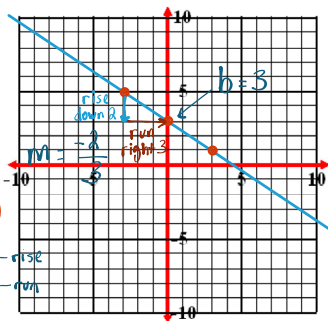
ex2) $y = -\frac{2}{3}x + 3$

$m = -\frac{2}{3}$

Alternatively, we could choose any 2 points from the table and use the slope formula to calculate slope of the line.

(It's still just rise/run) $m = \frac{y_2 - y_1}{x_2 - x_1}$

X	Y
0	3
3	1
-3	5



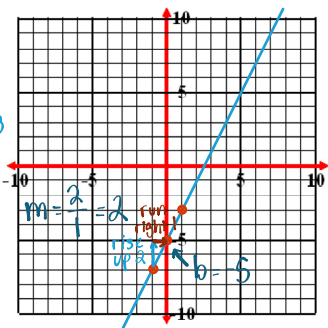
(y-intercept) $b = 3$

ex3) $y = 2x - 5$

$m = 2$

Do we notice anything when looking at an equation along with its slope and y-intercept?

X	Y
0	-5
1	-3
-1	-7



(y-intercept) $b = -5$

THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

When a linear equation is **solved for y**, the equation is written in **slope-intercept form**.

The Slope-Intercept Form

$$y = mx + b$$

↑
slope

↑
y-intercept

THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

Give the slope and the y-intercept of the following lines.

ex4) $y = -\frac{3}{4}x + 2$

$$y = m x + b$$

$$m = -\frac{3}{4}$$

$$b = 2$$

ex5) $y = 5x - 4$

$$y = m x + b$$

$$m = 5$$

$$b = -4$$

ex6) $y = 1x - \frac{1}{2}$

$$y = m x + b$$

$$m = 1$$

$$b = -\frac{1}{2}$$

ex7) $y = -4x + 0$

$$y = m x + b$$

$$m = -4$$

$$b = 0$$

THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

Give the slope and the y-intercept of the following lines.

ex8) $5y = -2x + 10$

ex9) $8x - 2y = 14$

Neither of these equations are in slope-intercept form. If we want to see the slope and y-intercept in each equation, we will have to convert to slope-intercept form by **SOLVING FOR Y**.

$$\frac{5y}{5} = \frac{-2x}{5} + \frac{10}{5}$$

$$y = -\frac{2}{5}x + 2$$

$$y = \underset{\uparrow}{m}x + \underset{\uparrow}{b}$$

$$m = -\frac{2}{5}$$

$$b = 2$$

$$\begin{array}{r} 8x - 2y = 14 \\ -8x \end{array}$$

$$\frac{-2y}{-2} = \frac{-8x}{-2} + \frac{14}{-2}$$

$$y = 4x - 7$$

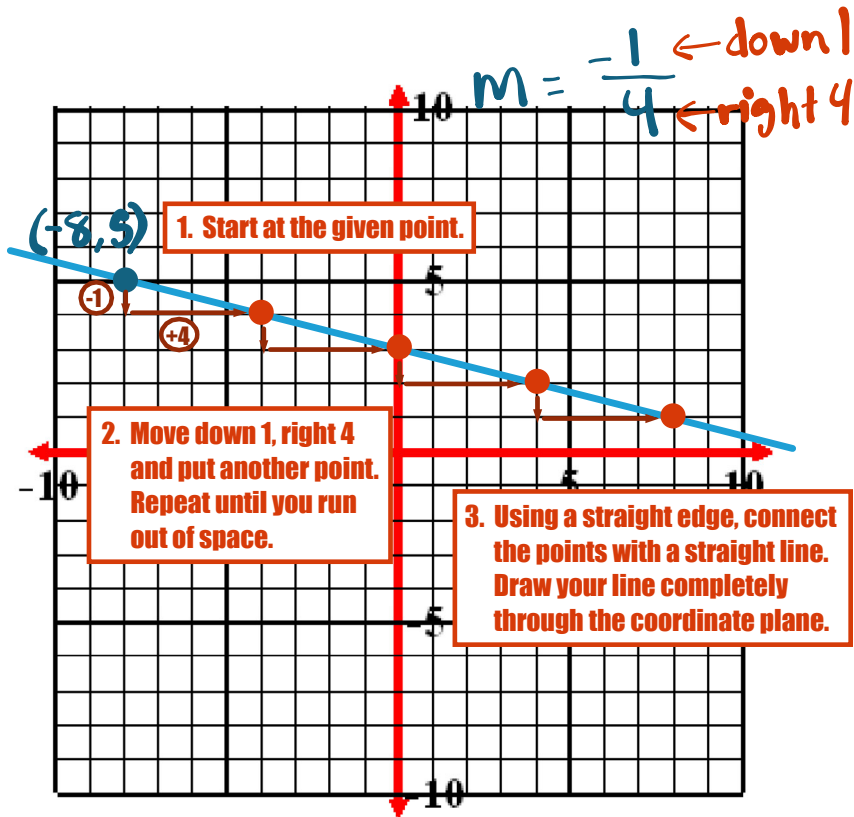
$$y = \underset{\uparrow}{m}x + \underset{\uparrow}{b}$$

$$m = 4$$

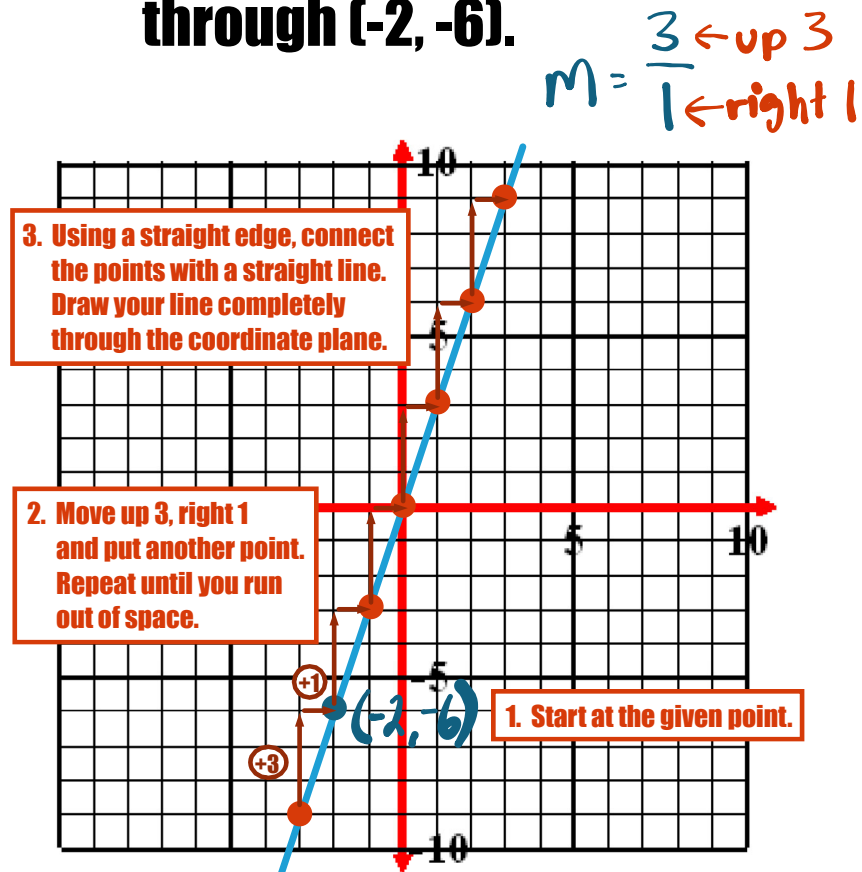
$$b = -7$$

THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

ex10) Graph the line that has a slope of $-\frac{1}{4}$ and passes through $(-8, 5)$.



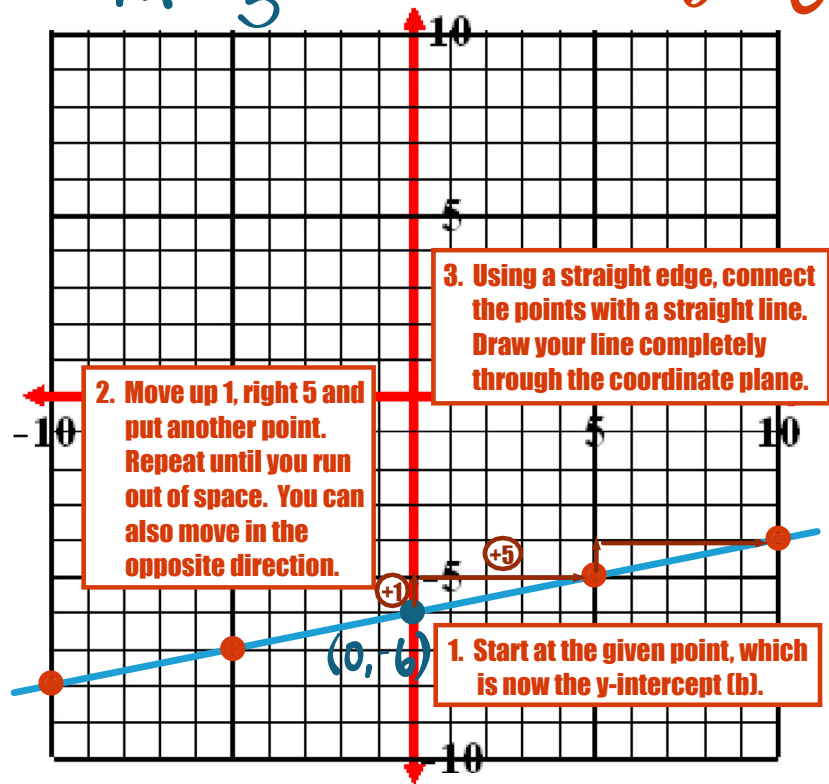
ex11) Graph the line that has a slope of 3 and passes through $(-2, -6)$.



THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

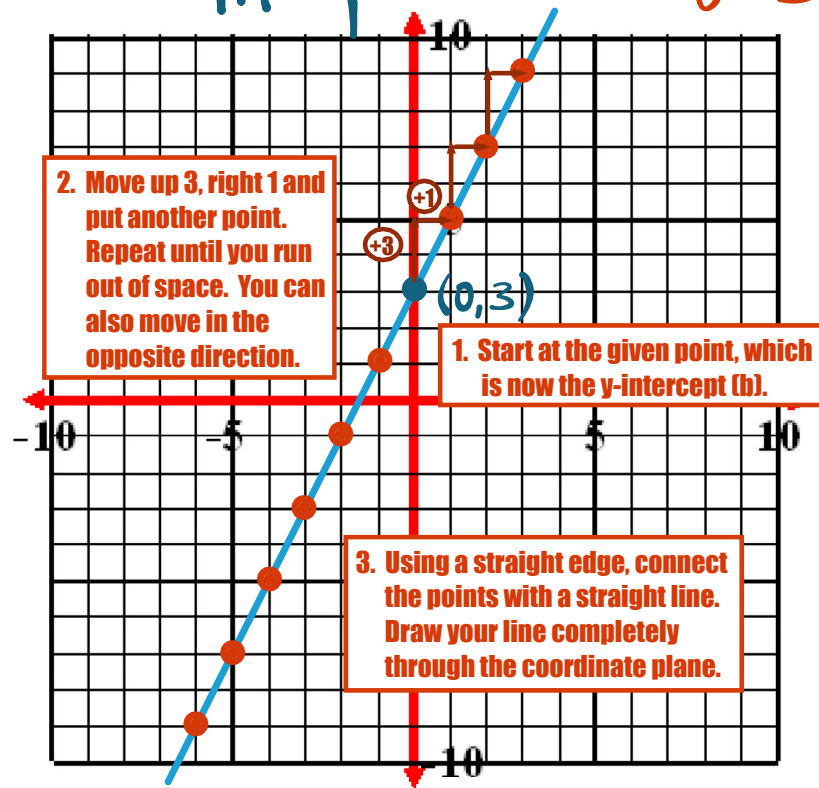
ex12) Graph: $y = \frac{1}{5}x - 6$

$m = \frac{1}{5}$ $b = -6$



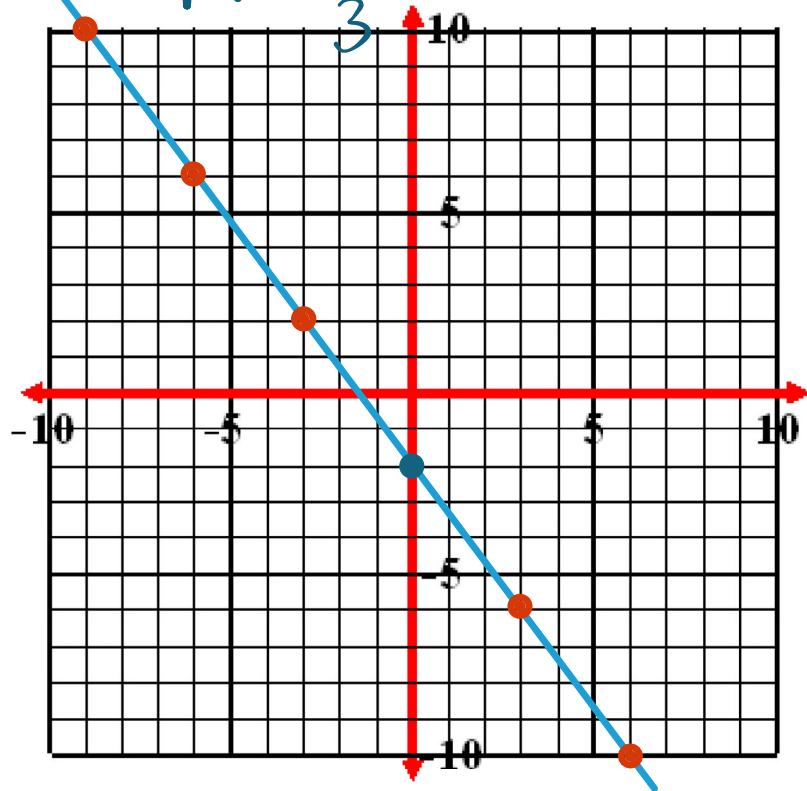
ex13) Graph: $y = 2x + 3$

$m = \frac{2}{1}$ $b = 3$

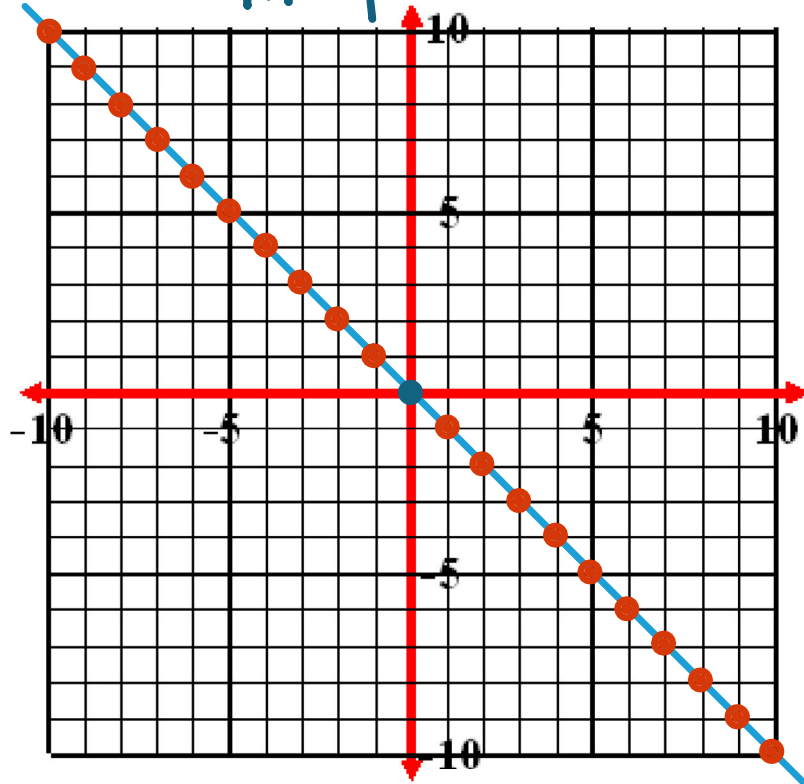


THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

ex14) Graph: $y = -\frac{4}{3}x - 2$
 $m = -\frac{4}{3}$ $b = -2$



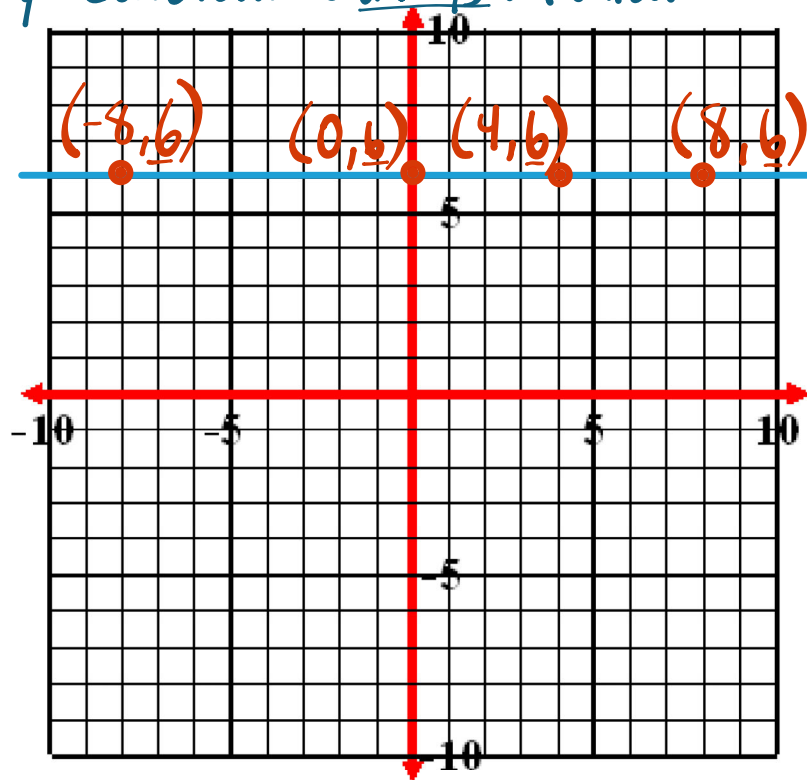
ex15) Graph: $y = -1x + 0$
 $m = -1$ $b = 0$



THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

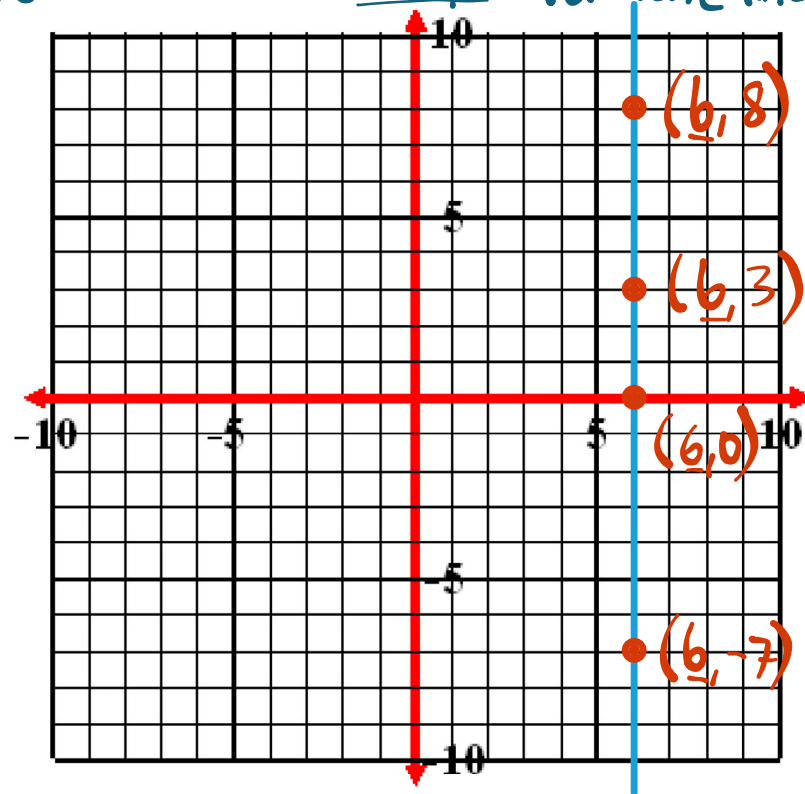
ex16) Graph: $y = 6$ (All points on this line have y-coordinate 6)

$y = \text{constant}$ is always a HORIZONTAL line.



ex17) Graph: $x = 6$ (All points on this line have x-coordinate 6)

$x = \text{constant}$ is always a VERTICAL line.



THE SLOPE-INTERCEPT FORM OF A LINEAR EQUATION

ex18) Graph: $6y - 5x = -6$ *Convert to slope-intercept form by solving for y!*

$$+5x \quad +5x$$

$$\frac{6y}{6} = \frac{5x}{6} - \frac{6}{6}$$

$$y = \frac{5}{6}x - 1$$

$$m = \frac{5}{6}$$

$$b = -1$$

