

ALL PROBLEMS CAN BE COMPLETED ON THIS WORKSHEET

WS 9C.1 - Solving Systems of Equations by Elimination

#1-8, Solve each system of equations by the elimination method.

$$1. \begin{cases} 2x - 3y = 6 \\ x + 3y = 12 \end{cases}$$

$$\underline{3x = 18}$$

$$\underline{x = 6}$$

$$x + 3y = 12$$

$$6 + 3y = 12$$

$$3y = 6$$

$$\underline{y = 2}$$

The solution
is (6, 2).

$$2. \begin{cases} 4x + 2y = 2 \xrightarrow{\cdot(-1)} -4x - 2y = -2 \\ 5x + 2y = 4 \longrightarrow 5x + 2y = 4 \end{cases}$$

$$\underline{x = 2}$$

$$4x + 2y = 2$$

$$4(2) + 2y = 2$$

$$8 + 2y = 2$$

$$2y = -6$$

$$\underline{y = -3}$$

The solution
is (2, -3).

$$3. \begin{cases} 3x + 2y = 8 \xrightarrow{\cdot 3} 9x + 6y = 24 \\ 2x - 6y = 42 \longrightarrow 2x - 6y = 42 \end{cases}$$

$$\underline{11x = 66}$$

$$\underline{x = 6}$$

$$3x + 2y = 8$$

$$3(6) + 2y = 8$$

$$18 + 2y = 8$$

$$2y = -10$$

$$\underline{y = -5}$$

The solution
is (6, -5).

$$4. \begin{cases} 3x + 4y = 22 \longrightarrow 3x + 4y = 22 \\ x - 5y = -37 \xrightarrow{\cdot(-3)} -3x + 15y = 111 \end{cases}$$

$$19y = 133$$

$$\underline{y = 7}$$

$$3x + 4y = 22$$

$$3x + 4(7) = 22$$

$$3x + 28 = 22$$

$$3x = -6$$

$$\underline{x = -2}$$

The solution
is (-2, 7).

$$5. \begin{cases} 2x - 5y = -19 & \xrightarrow{\cdot 2} 4x - 10y = -38 \\ 3x + 2y = 0 & \xrightarrow{\cdot 5} 15x + 10y = 0 \end{cases}$$

$$\begin{array}{r} 4x - 10y = -38 \\ 15x + 10y = 0 \\ \hline 19x = -38 \\ x = -2 \end{array}$$

$$\begin{array}{l} 3x + 2y = 0 \\ 3(-2) + 2y = 0 \\ -6 + 2y = 0 \\ 2y = 6 \\ y = 3 \end{array}$$

The solution is $(-2, 3)$.

$$6. \begin{cases} x - 2y = 11 \\ 2y + 8 = -2x \end{cases}$$

Rearrange terms.

$$\begin{array}{l} x - 2y = 11 \\ 1 - 2y = 11 \\ -2y = 10 \\ y = -5 \end{array}$$

$$\begin{array}{l} x - 2y = 11 \\ 2x + 2y = -8 \\ \hline 3x = 3 \\ x = 1 \end{array}$$

The solution is $(1, -5)$.

$$7. \begin{cases} 2x - 3y = 6 & \xrightarrow{\cdot (-3)} -6x + 9y = -18 \\ 6x - 9y = 9 & \longrightarrow 6x - 9y = 9 \end{cases}$$

$$\begin{array}{r} -6x + 9y = -18 \\ 6x - 9y = 9 \\ \hline 0 = -9 \end{array}$$

There is no solution to this system.

(These lines are parallel.)

$$8. \begin{cases} 7x + 5y = -2 & \xrightarrow{\cdot 3} 21x + 15y = -6 \\ -21x - 15y = 6 & \longrightarrow -21x - 15y = 6 \end{cases}$$

$$\begin{array}{r} 21x + 15y = -6 \\ -21x - 15y = 6 \\ \hline 0 = 0 \end{array}$$

Solve for y : $7x + 5y = -2$

$$5y = -7x - 2$$

$$y = \underline{\underline{-\frac{7}{5}x - \frac{2}{5}}}$$

Infinitely many solutions. All points on the line $y = -\frac{7}{5}x - \frac{2}{5}$ are solutions to the system.

(These two lines are the same line.)