

ALL PROBLEMS CAN BE COMPLETED ON THIS WORKSHEET

WS 15.1 - Word Problems Involving Linear Equations

Solve each problem. Remember to answer in complete sentences.

1. Alex has some quarters and \$5.15 in nickels. If he has \$7.90 total, how many quarters does he have?

let q = number of quarters Alex has

$$\begin{array}{r}
 \$ \text{ in quarters} + \$ \text{ in nickels} = \$ \text{ total} \\
 0.25q + 5.15 = 7.90 \\
 \begin{array}{r}
 0.25q + 5.15 = 7.90 \\
 - 5.15 \quad - 5.15 \\
 \hline
 0.25q = 2.75 \\
 \frac{0.25q}{0.25} = \frac{2.75}{0.25} \\
 q = 11
 \end{array}
 \end{array}$$

25¢ times number of quarters

$q = 11$
 Alex has 11 quarters.

2. Twelve decreased by the quotient of a number and -2 is 15. Find the number.

let n = the number

$$\begin{array}{r}
 12 - \frac{n}{-2} = 15 \implies 12 + \frac{n}{2} = 15 \\
 \begin{array}{r}
 12 + \frac{n}{2} = 15 \\
 -12 \quad -12 \\
 \hline
 \frac{n}{2} = 3 \\
 \frac{n}{2} \cdot 2 = 3 \cdot 2 \\
 n = 6
 \end{array}
 \end{array}$$

$n = 6$
 The number is 6.

3. An Internet service provider offers internet access for \$15.75 per month with a \$29.95 initial charge for the hookup. If Glenda spent a total of \$187.45 on her Internet access, how many months did she pay for?

let m = number of months Glenda paid for

$$\begin{array}{r}
 15.75m + 29.95 = 187.45 \\
 \begin{array}{r}
 15.75m + 29.95 = 187.45 \\
 - 29.95 \quad - 29.95 \\
 \hline
 15.75m = 157.50 \\
 \frac{15.75m}{15.75} = \frac{157.50}{15.75} \\
 m = 10
 \end{array}
 \end{array}$$

$m = 10$
 Glenda paid for 10 months.

4. If 11.2 less than the average of 5 numbers is 27.75, what is the sum of the 5 numbers?

let s = sum of the 5 numbers

$$\begin{array}{r}
 \frac{\text{sum of the 5 numbers}}{5} - 11.2 = 27.75 \\
 \begin{array}{r}
 \frac{s}{5} - 11.2 = 27.75 \\
 + 11.2 \quad + 11.2 \\
 \hline
 \frac{s}{5} = 38.95 \\
 s = 194.75
 \end{array}
 \end{array}$$

average of 5 numbers

$\frac{s}{5} = 38.95$
 $s = 194.75$
 The sum of the 5 numbers is 194.75.

5. Five times a number subtracted from 3 times the number is 20. Find the number.

let $n =$ the number

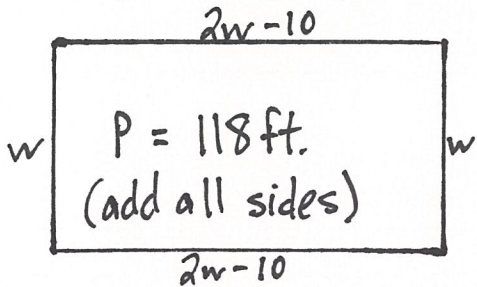
$$\underline{3n} - 5n = 20$$

$$\begin{array}{r} -2n = 20 \\ \underline{-2} \quad \underline{-2} \end{array}$$

$$n = -10$$

The number is -10 .

6. The length of a rectangular sign is 10 ft. less than twice its width. Find the length and width of the sign if its perimeter is 118 ft.



let $w =$ width
then $2w - 10 =$ length

$$P = \underline{w} + \underline{w} + \underline{2w - 10} + \underline{2w - 10}$$

$$118 = 6w - 20$$

$$\begin{array}{r} +20 \quad +20 \\ \underline{138} = \underline{6w} \\ \underline{6} \quad \underline{6} \end{array} \Rightarrow w = 23$$

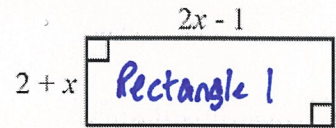
The width is 23 ft.

$$2w - 10 = 2(23) - 10 = 36$$

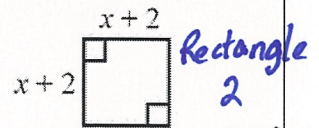
The length is 36 ft.

7. The perimeters of the two rectangles shown are equal. Find the value of x and the perimeter of the rectangles.

$$\begin{aligned} \text{Rectangle 1} &= \underline{2x-1} + \underline{2x-1} + \underline{2+x} + \underline{2+x} \\ &= \underline{6x+2} \end{aligned}$$



$$\begin{aligned} \text{Rectangle 2} &= \underline{x+2} + \underline{x+2} + \underline{x+2} + \underline{x+2} \\ &= \underline{4x+8} \end{aligned}$$



Rectangle Perimeters are equal \rightarrow

$$\begin{array}{r} 6x + 2 = 4x + 8 \\ \underline{-4x} \quad \underline{-4x} \\ 2x + 2 = 8 \\ \underline{-2} \quad \underline{-2} \end{array} \rightarrow \begin{array}{r} 2x = 6 \\ \underline{2} \quad \underline{2} \\ x = 3 \end{array}$$

$$\text{Rect 1} = 6(3) + 2 = 20 \text{ ft}$$

$$\text{Rect 2} = 4(3) + 8 = 20 \text{ ft}$$

8. The product of 3 and the sum of a number and 5, then added to 6 is the same as the product of -2 and 3 decreased by the number, then minus 5. Find the number.

let $n =$ the number

$$3(n+5) + 6 = -2(3-n) - 5$$

$$\underline{3n} + \underline{15} + \underline{6} = \underline{-6} + \underline{2n} - \underline{5}$$

$$\begin{array}{r} 3n + 21 = 2n - 11 \\ \underline{-2n} \quad \underline{-2n} \end{array}$$

$$\begin{array}{r} n + 21 = -11 \\ \underline{-21} \quad \underline{-21} \end{array} \rightarrow n = -31$$

The number is -31 .