

To Clear Fractions: ① Get common denominator  
② Multiply every term in equation by common denominator

Pre-Algebra B

Name/Date **solutions**

## WS 20.1 - Solving Special Equations

Solve each equation by clearing fractions.

$$1. \frac{x}{2} + \frac{5x}{6} = \frac{1}{9}$$

$$9x + 15x = 2$$

$$24x = 2$$

$$x = \frac{2}{24}$$

$$\boxed{x = \frac{1}{12}}$$

$$2. \frac{n-2}{5} + \frac{n}{3} = \frac{n}{2} + 1$$

$$6(n-2) + 10n = 15n + 30$$

$$6n - 12 + 10n = 15n + 30$$

$$16n - 12 = 15n + 30$$

$$-15n \quad -15n$$

$$n - 12 = 30$$

$$\boxed{n = 42}$$

$$3. 2d - 2 = \frac{d}{3} - \frac{5d}{6} - \frac{7d}{2}$$

$$12d - 12 = 2d - 5d - 21d$$

$$12d - 12 = -24d$$

$$-12d \quad -12d$$

$$-12 = -36d$$

$$\frac{-12}{-36} = d$$

$$\frac{1}{3} = d \Rightarrow \boxed{d = \frac{1}{3}}$$

$$4. \frac{4m}{7} - 3(m-2) + \frac{m}{2} = \frac{5m}{4} - \frac{m}{7} + 1$$

$$\frac{4m}{7} - 3m + 6 + \frac{m}{2} = \frac{5m}{4} - \frac{m}{7} + 1$$

$$16m - 84m + 168 + 14m = 35m - 4m + 28$$

$$-54m + 168 = 31m + 28$$

$$-31m \quad -31m$$

$$-85m + 168 = 28$$

$$-85m = -140$$

$$m = \frac{-140}{-85}$$

$$\boxed{m = \frac{28}{17}}$$

$$5. 2(3x-1) + \frac{3x}{8} - \frac{1}{6} = \frac{x}{4} - \frac{2}{3}(6x-12)$$

$$6x - 2 + \frac{3x}{8} - \frac{1}{6} = \frac{x}{4} - 4x + 8$$

$$144x - 48 + 9x - 4 = 6x - 96x + 192$$

$$153x - 52 = -90x + 192$$

$$+90x \quad +90x$$

$$243x - 52 = 192$$

$$243x = 244$$

$$\boxed{x = \frac{244}{243}}$$

When all variables cancel out: If equation is true (balanced scale)  $\rightarrow$  infinitely many solutions  
 If equation is false (unbalanced scale)  $\rightarrow$  no solution

Solve each equation.

6.  $2y - 4 = 2(y - 3)$

$$\begin{array}{rcl} 2y - 4 & = & 2y - 6 \\ -2y & & -2y \\ -4 & = & -6 \end{array}$$

Variables have cancelled and equation is false.

No Solution

7.  $2y - 4 = 2(y - 2)$

$$\begin{array}{rcl} 2y - 4 & = & 2y - 4 \\ -2y & & -2y \\ -4 & = & -4 \end{array}$$

Variables have cancelled and equation is true.

Infinitely many solutions.  
 (All numbers work)

8.  $-4 + 5(x + 1) = 2x + 3(x + 1)$

$$\begin{array}{rcl} -4 + 5x + 5 & = & 2x + 3x + 3 \\ 5x + 1 & = & 5x + 3 \\ -5x & & -5x \\ 1 & = & 3 \end{array}$$

Variables have cancelled and equation is false.

No Solution

9.  $6(4 - 2x) = -2(5x - 5) - 2x$

$$\begin{array}{rcl} 24 - 12x & = & -10x + 10 - 2x \\ 24 - 12x & = & -12x + 10 \\ +12x & & +12x \\ 24 & = & 10 \end{array}$$

Variables have cancelled and equation is false.

No Solution

10.  $5 + \frac{k}{2} + \frac{k}{4} = \frac{3k}{2} + 5 - \frac{3k}{4}$  Clear fractions!

$$\begin{array}{rcl} 20 + 2k + k & = & 6k + 20 - 3k \\ 20 + 3k & = & 3k + 20 \\ -3k & & -3k \\ 20 & = & 20 \end{array}$$

Variables have cancelled and equation is true.

Infinitely many solutions  
 (All numbers work)